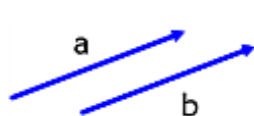


VECTORS: A GEOMETRIC APPROACH

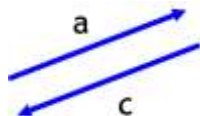
- OBJECTIVES:** 1) Draw a vector in the coordinate plane and compute its magnitude (two different ways).
 2) Determine the resultant of two forces.
 3) Find the horizontal and vertical components of a vector.

VECTOR BASICS

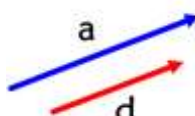
Many physical quantities such as length, area, volume, or speed can be completely specified by a single real number, which we call **scalar quantities**. Other quantities, such as velocities and forces require for their complete specification both a magnitude and a direction, which we call **vector quantities**.



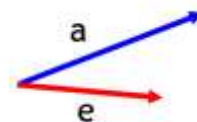
Same magnitude and direction: $\mathbf{a} = \mathbf{b}$



Same magnitude, directions are not the same: $\mathbf{a} \neq \mathbf{b}$



Same direction, magnitudes are not the same: $\mathbf{a} \neq \mathbf{d}$



Neither magnitude nor direction are the same: $\mathbf{a} \neq \mathbf{e}$

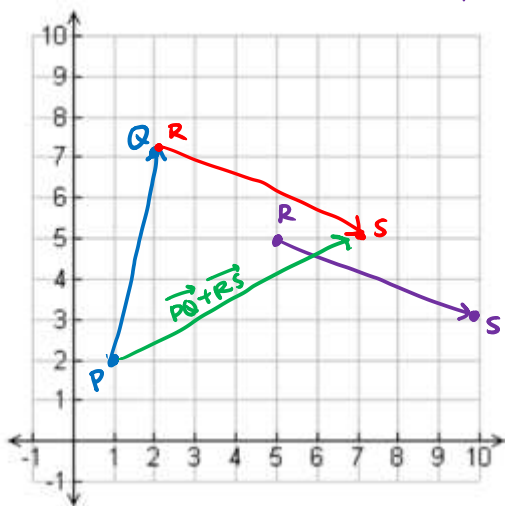
VECTOR ADDITION

Two different approaches:

Given the following points, draw the vector $\overrightarrow{PQ} + \overrightarrow{RS}$ and compute its magnitude.

$$P(1,2) \quad Q(2,7) \quad R(5,5) \quad S(10,3)$$

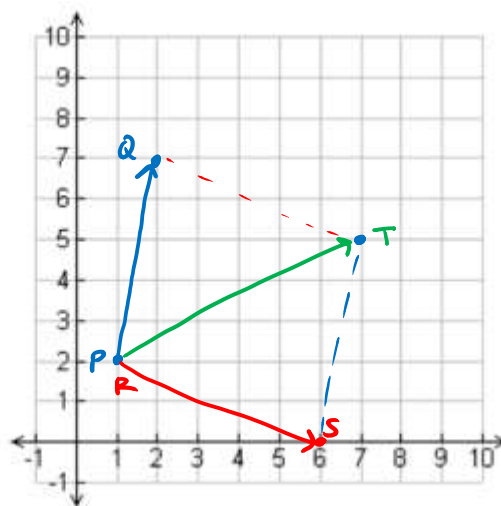
HEAD-TO-TAIL RULE



$$\overrightarrow{PT} \quad P(1,2) \quad T(7,5)$$

$$\begin{aligned} |\overrightarrow{PQ} + \overrightarrow{RS}| &= \sqrt{(1-7)^2 + (2-5)^2} \\ &= \sqrt{36 + 9} \\ &= \sqrt{45} \\ &= \boxed{3\sqrt{5}} \end{aligned}$$

PARALLELOGRAM RULE

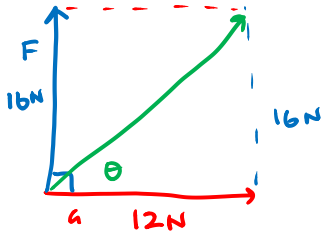


$$\overrightarrow{PT} \quad P(1,2) \quad T(7,5)$$

$$|\overrightarrow{PT}| = |\overrightarrow{PQ} + \overrightarrow{RS}| = 3\sqrt{5}$$

THE RESULTANT OF TWO PERPENDICULAR FORCES

Two forces **F** and **G** act on an object. **G** acts horizontally to the right with a magnitude of 12 N (newtons, $1\text{N} \approx 0.2248\text{lb.}$). **F** acts vertically upward with a magnitude of 16 N. Determine the magnitude and direction of the resultant force.



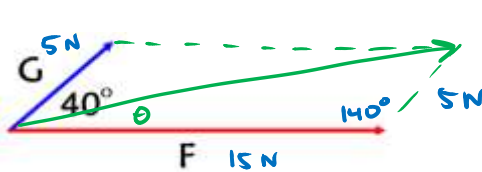
$$|F+G| = \sqrt{12^2 + 16^2} = \sqrt{400} = 20\text{ N}$$

$$\tan \theta = \frac{16}{12}$$

$$\theta = \tan^{-1}\left(\frac{16}{12}\right) \quad \theta \approx 53.1^\circ$$

THE RESULTANT OF TWO FORCES

Force **F** acts on an object horizontally to the right with a magnitude of 15 N. Force **G** acts on the object as indicated in the diagram with a magnitude of 5 N. Determine the resultant of the two forces.



$$|F+G| = \sqrt{5^2 + 15^2 - 2(5)(15)\cos 140^\circ}$$

$$|F+G| \approx 19.1\text{ N}$$

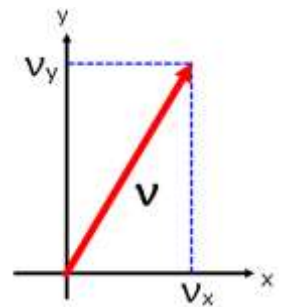
STORE THIS!

$$\frac{\sin \theta}{5\text{ N}} = \frac{\sin 140^\circ}{19.1\text{ N}} \quad \leftarrow \text{STORE!}$$

$$\sin \theta = \frac{5 \sin 140^\circ}{19.1}$$

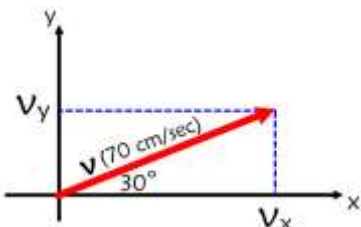
$$\theta = \sin^{-1}\left(\frac{5 \sin 140^\circ}{19.1}\right)$$

$$\theta \approx 9.7^\circ$$



FINDING HORIZONTAL AND VERTICAL COMPONENTS

Determine the horizontal and vertical components of the velocity vector in the figure below.



$$\sin 30^\circ = \frac{V_y}{70}$$

$$\cos 30^\circ = \frac{V_x}{70}$$

$$V_y = 70 \sin 30^\circ$$

$$V_x = 70 \cos 30^\circ$$

$$V_y = 35\text{ cm/sec}$$

$$V_x = 70 \cdot \frac{\sqrt{3}}{2}$$

$$V_x = 35\sqrt{3}\text{ cm/sec}$$