

7.8 NOTES – SUMS AND DIFFERENCES OF RATIONAL EXPRESSIONS

OBJECTIVES:

- 1) Determine the least common multiple (LCM) of polynomials
- 2) Add and subtract rational expressions

WARM-

Evaluate without the use of a calculator: $\frac{3}{2} + \frac{1}{7} = \frac{21}{14} + \frac{2}{14} = \boxed{\frac{23}{14}}$ Find the LCM: 3, 5, 9 45

LEAST COMMON MULTIPLE:

a) $15x^2, 24x$

$120x^2$

b) $3x^2y^2, 5xy^3, 2xy$

$30x^2y^3$

c) $z+1, z-1$

z^2-1 or $(z-1)(z+1)$

d) $n^2-7n+12, n^2-2n-8$

$(n-4)(n-3), (n-4)(n+2)$
 $(n-4)(n-3)(n+2)$

ADDING AND SUBTRACTING RATIONAL EXPRESSIONS

1) $\frac{x}{4} + \frac{5x}{4} = \frac{6x}{4} = \boxed{\frac{3x}{2}}$

2) $\frac{x+1}{3y^2} - \frac{x+1}{-3y^2}$

$\frac{x+1}{3y^2} + \frac{x+1}{3y^2} = \frac{2(x+1)}{3y^2}$

3) $\frac{3}{5x^2} + \frac{7}{10x}$

$\frac{6}{10x^2} + \frac{7x}{10x^2}$

$\frac{7x+6}{10x^2}$

4) $\frac{7x}{15y^2} - \frac{y}{18xy}$

$\frac{42x^2}{90xy^2} - \frac{5y^2}{90xy^2} = \frac{42x^2-5y^2}{90xy^2}$

$$5) \frac{3}{2a+4} + \frac{4}{a^2+2a}$$

$$\frac{3}{2(a+2)} + \frac{4}{a(a+2)}$$

$$\frac{3a}{2a(a+2)} + \frac{4(2)}{2a(a+2)}$$

$$\boxed{\frac{3a+8}{2a(a+2)}}$$

$$6) \frac{2x-6}{x-1} - \frac{4}{1-x}$$

$$\frac{2x-6}{x-1} + \frac{4}{x-1}$$

$$\frac{2x-2}{x-1}$$

$$\frac{2(x-1)}{(x-1)} = \boxed{2}$$

$$7) \frac{3m-26}{m-6} + \frac{8}{6-m}$$

$$\frac{3m-26}{m-6} - \frac{8}{m-6}$$

$$\boxed{\frac{3m-34}{m-6}}$$

$$8) \frac{y+3}{y-2} - \frac{4y-13}{y^2-5y+6}$$

$$\frac{(y-3) \cdot y+3}{(y-3)(y-2)} - \frac{4y-13}{(y-3)(y-2)}$$

$$\frac{y^2-9}{(y-2)(y-3)} - \frac{4y-13}{(y-3)(y-2)}$$

$$\frac{y^2-9-(4y-13)}{(y-3)(y-2)} = \frac{y^2-4y+4}{(y-3)(y-2)(y-2)(y+3)} = \frac{(y-2)^2}{(y-3)(y-2)(y-2)(y+3)}$$

$$= \boxed{\frac{y-2}{y+3}}$$

$$9) \frac{2}{x+1} + \frac{2}{x-1} + \frac{1}{x^2-1}$$

$$\frac{(x-1) \cdot 2}{(x-1)(x+1)} + \frac{2 \cdot (x+1)}{(x-1)(x+1)} + \frac{1}{x^2-1} \leftarrow (x+1)(x-1)$$

$$\frac{2(x-1)}{(x-1)(x+1)} + \frac{2(x+1)}{(x-1)(x+1)} + \frac{1}{x^2-1}$$

$$\frac{2x-2+2x+2+1}{(x+1)(x-1)} = \boxed{\frac{4x+1}{(x+1)(x-1)}}$$

$$10) \frac{\frac{1}{x} + \frac{1}{y}}{\frac{1}{xy}} \cdot \frac{xy}{xy}$$

$$\frac{\frac{xy}{x} + \frac{xy}{y}}{\frac{xy}{xy}} = \frac{y+x}{1} = \boxed{x+y}$$