

GRAPH RATIONAL FUNCTIONS AND REVIEW STUFF

Name _____

Date _____ Period _____

Fill in all the information, and graph each rational function.

1) $f(x) = \frac{x^3 + 3x^2 - x - 3}{x+1}$

$$f(x) \frac{x^2(x+3) - 1(x+3)}{x+1} = \frac{(x^2-1)(x+3)}{(x+1)} = \frac{(x-1)(x+1)(x+3)}{(x+1)}$$

$f(x) = (x-1)(x+3)$ Quadratic!

$= x^2 + 2x - 3$

vertex: $-\frac{b}{2a} = \frac{-2}{2(1)} = -1$
 $(-1, -4)$

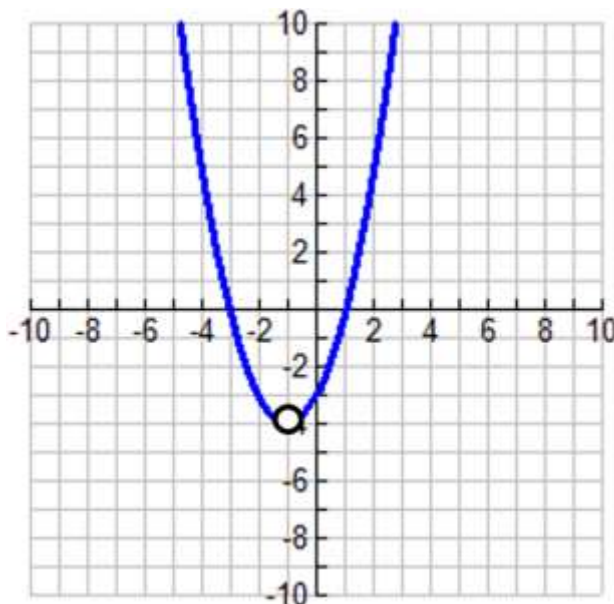
hole(s): $(-1, -4)$

x-int: $(1, 0)(-3, 0)$

y-int: $(0, -3)$

VA: DNE

HA: DNE



2) $f(x) = \frac{2x^2 - 2x - 24}{x^2 + x - 12} = \frac{2(x^2 - x - 12)}{(x^2 + x - 12)} = \frac{2(x-4)(x+3)}{(x+4)(x-3)}$

x int: $y=0$

$$0 = \frac{2(x-4)(x+3)}{(x+4)(x-3)}$$

$$0 = 2(x-4)(x+3)$$

$x = 4, -3$

y int: $x=0$

$$f(0) = \frac{2(-4)(3)}{(4)(-3)}$$

$$f(0) = 2$$

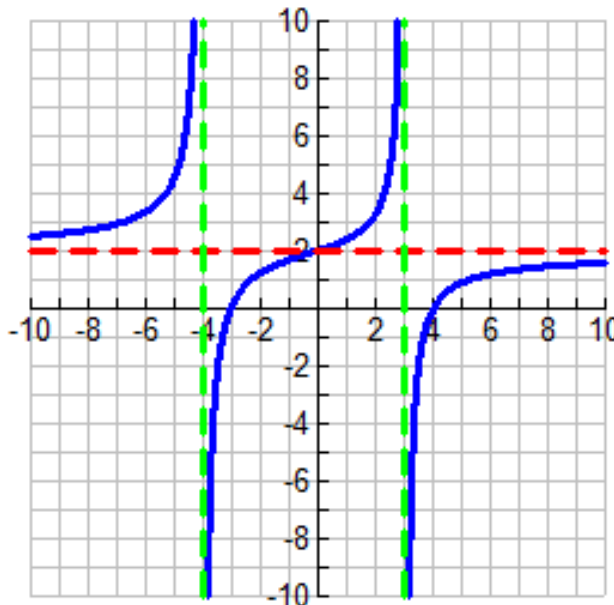
hole(s): DNE

x-int: $(4, 0)(-3, 0)$

y-int: $(0, 2)$

VA: $x = -4$ $x = 3$

HA: $y = 2$



$$3) f(x) = \frac{(x+5)^2(x-1)}{(x-1)(x+2)(x-3)^2}$$

$$f(x) = \frac{(x+5)^2}{(x+2)(x-3)^2}$$

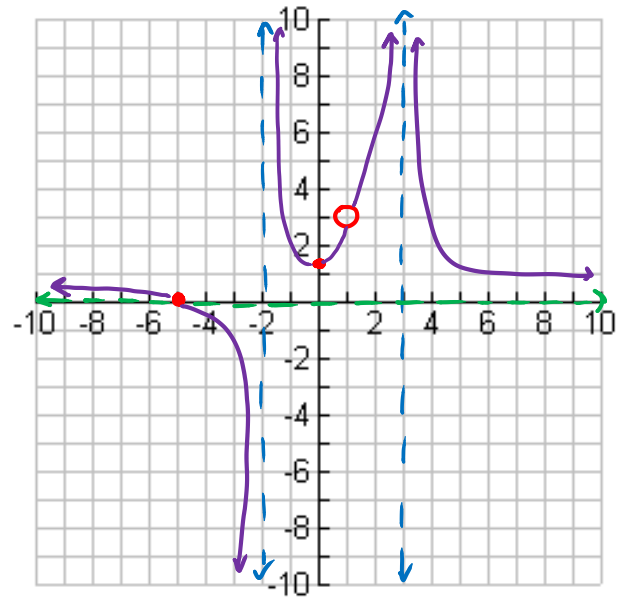
hole(s): $(1, 3)$

x - int: $(-5, 0)$

y - int: $(0, \frac{25}{10})$

VA: $x = -2$ $x = 3$

HA: $y = 0$



$$4) f(x) = \frac{x^2 + x - 6}{x^2 + 5x + 6} = \frac{(x-3)(x+2)}{(x+3)(x+2)}$$

$$f(x) = \frac{x-3}{x+3}$$

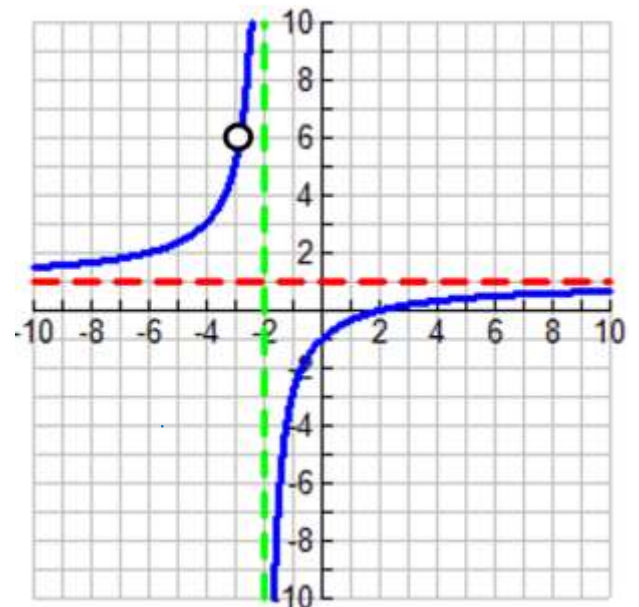
hole(s): $(-3, 5)$

x - int: $(2, 0)$

y - int: $(0, -1)$

VA: $x = -2$

HA: $y = 1$



$$5) f(x) = \frac{(x-1)(\cancel{x-4})}{(\cancel{x-4})(x-3)(x+2)}$$

$$f(x) = \frac{(x-1)}{(x-3)(x+2)}$$

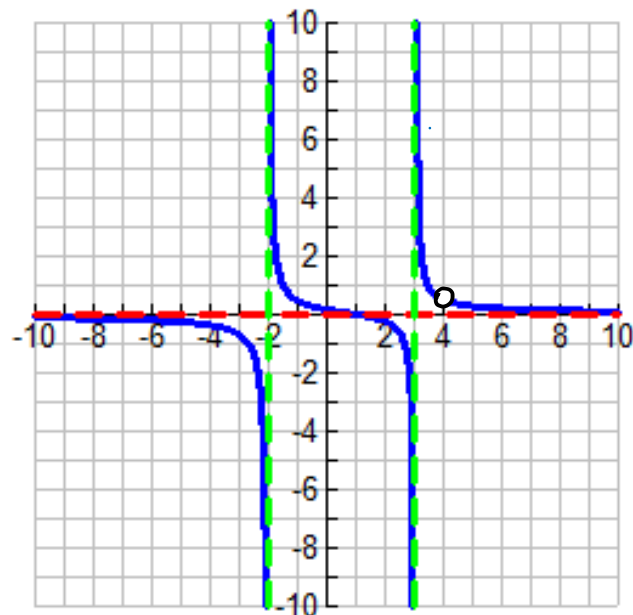
hole(s): $(4, \frac{1}{2})$

x - int: $(1, 0)$

y - int: $(0, \frac{1}{6})$

VA: $x=3$ $x=-2$

HA: $y=0$



$$6) f(x) = \frac{(x-1)(x+3)}{(x+1)^2(x-3)}$$

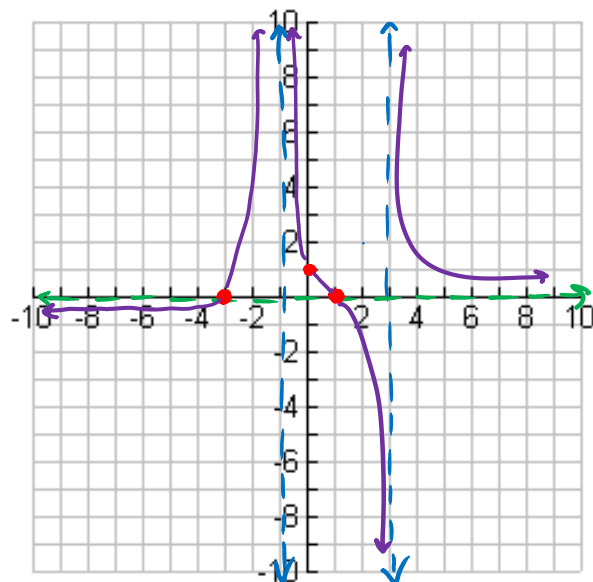
hole(s): DNE

x - int: $(1, 0)$ $(-3, 0)$

y - int: $(0, 1)$

VA: $x=-1$ $x=3$

HA: $y=0$



7. Given the sets of data below: 1) Name the type of function that best fits the data, and 2) Write the particular equation that fits the data.

A) B) C) D)

x	y
1	-2
3	22
5	70
7	142
9	238

x	y
-8	13122
-6	1458
-4	162
-2	18
0	2

x	y
0	4
3	6
6	8
9	10

x	y
1	4
2	1
4	.25
8	.0625

Quadratic:
 (use 3 pts in $ax^2+bx+c=y$)
 then use matrix

$$\begin{bmatrix} 1 & 1 & 1 & -2 \\ 9 & 3 & 1 & 22 \\ 25 & 5 & 1 & 70 \end{bmatrix} \xrightarrow{\text{RREF}} \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -5 \end{bmatrix}$$

$y = 3x^2 - 5$

Exponential:
 $y = a(b)^x$
 $y = 2(b)^x$
 $18 = 2(b)^{-2}$
 $b = \frac{1}{3}$

$y = 2\left(\frac{1}{3}\right)^x$

Linear: $\frac{\Delta y}{\Delta x} = \frac{2}{3}$
 $b = 4$

$y = \frac{2}{3}x + 4$

Inverse Variation:
 $y = \frac{k}{x^2}$
 $4 = \frac{k}{1^2}$
 $k = 4$

$y = \frac{4}{x^2}$

8. You are looking to buy a new car and decide to do some research about the depreciation of the cars. Your first choice has a purchase price of \$42,000, but its value decreases by 30% each year. Your second, more affordable but not as sporty, choice has a purchase price of \$25,000 and will only depreciate by 15% each year.

a) How much will each car be worth in 2 years? 5 years? 10 years?

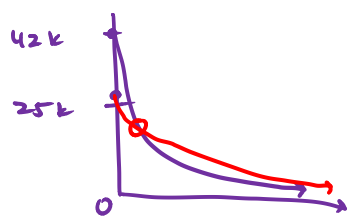
$$y_1 = 42,000(1-.30)^x \quad y_2 = 25,000(1-.15)^x$$

Car 1: @ 2 yrs: \$20,580 Car 2: \$18,062.50
 @ 5 yrs: \$7,058.94 \$11,092.63
 @ 10 yrs: \$1,106.40 \$4,921.86

b) Write an equation to represent the value of each car after n years.

$$y = 42,000(.7)^n \quad y = 25,000(.85)^n$$

c) Draw a quick sketch of each equation to answer the following question.



d) How long before the cars are worth the same amount?

$$42,000(.7)^x = 25,000(.85)^x \approx 2.67 \text{ yrs they are worth } \$16,193.$$

9. a. Write a general equation for: y varies inversely with the square of x .

$$y = \frac{k}{x^2}$$

- b. What happens to the value of y when x is tripled, in the variation above?

y decreases by a factor of $\frac{1}{9}$ / y is multiplied by a factor of $\frac{1}{9}$

10. a. Write a general equation for: y varies directly with the cube of x .

$$y = kx^3$$

- b. What happens to the value of y when x is multiplied by one-fifth, in the variation above?

y will decrease by a factor of $\frac{1}{125}$ / y will be multiplied by a factor of $\frac{1}{125}$

11. **The points (7, 45) and (21, 5) fit a variation function.**

- a. Which kind of variation function does the data represent?

Inverse Variation

$$.3 < \frac{7}{21} \mid \frac{45}{5} > \cdot \frac{1}{9}$$

- b. Write the particular equation for the function.

$$y = \frac{k}{x^2}$$

$$45 = \frac{k}{49}$$

$$k = 2205$$

$$y = \frac{2205}{x^2}$$

12. The mass of an orange varies directly with the cube of its diameter. If a Florida orange has twice the diameter of a California orange and the Florida orange weighs 6 oz. How much does the California orange weigh?

d = diameter

m = mass

$$m = k \cdot d^3$$

If d is cut in half, then mass is decreased by a factor of $\frac{1}{8}$.

So the mass of the California orange is $\frac{1}{8}$ times smaller than the Florida orange.

$$m = 6 \cdot \frac{1}{8} = \boxed{\frac{3}{4} \text{ oz.}} \leftarrow \text{Answer}$$