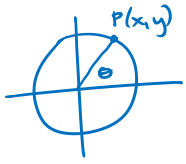


PROVE IT NOTES

I. BASIC DEFINITIONS

7 pts



1) $\cos \theta = x$

2) $\sin \theta = y$

3) $\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{y}{x}$

4) $\sec \theta = \frac{1}{\cos \theta} = \frac{1}{x}$

5) $\csc \theta = \frac{1}{\sin \theta} = \frac{1}{y}$

6) $\cot \theta = \frac{\cos \theta}{\sin \theta} = \frac{x}{y}$

II. PYTHAGOREAN IDENTITIES

5 pts

$$x^2 + y^2 = 1$$



7) $\cos^2 \theta + \sin^2 \theta = 1$

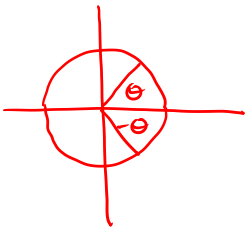
$$\frac{\cos^2 \theta + \sin^2 \theta}{\cos^2 \theta} = \frac{1}{\cos^2 \theta}$$

8) $1 + \tan^2 \theta = \sec^2 \theta$

$$\frac{\cos^2 \theta + \sin^2 \theta}{\sin^2 \theta} = \frac{1}{\sin^2 \theta}$$

9) $\cot^2 \theta + 1 = \csc^2 \theta$

III. OPPOSITE ANGLES



10) $\sin(-\theta) = -\sin \theta$

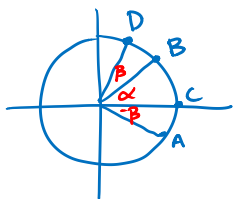
11) $\cos \theta = \cos(-\theta)$

$$\tan(-\theta) = \frac{\sin(-\theta)}{\cos(-\theta)} = \frac{-\sin \theta}{\cos \theta} = -\tan \theta$$

12) $\tan(-\theta) = -\tan \theta$

IV. ANGLE ADDITION

8 pts



$$A(\cos \beta, -\sin \beta) \quad B(\cos \alpha, \sin \alpha) \quad C(1, 0) \quad D(\cos(\alpha + \beta), \sin(\alpha + \beta))$$

$$AB = CD$$

$$\sqrt{(\cos \alpha - \cos \beta)^2 + (\sin \alpha + \sin \beta)^2} = \sqrt{(\cos(\alpha + \beta) - 1)^2 + \sin^2(\alpha + \beta)}$$

$$\cos^2 \alpha - 2\cos \alpha \cos \beta + \cos^2 \beta + \sin^2 \alpha + 2\sin \alpha \sin \beta + \sin^2 \beta = \cos^2(\alpha + \beta) - 2\cos(\alpha + \beta) + 1 + \sin^2(\alpha + \beta)$$

$$-2\cos \alpha \cos \beta + 2\sin \alpha \sin \beta + 2 = 2 - 2\cos(\alpha + \beta)$$

$$-2\cos \alpha \cos \beta + 2\sin \alpha \sin \beta = -2\cos(\alpha + \beta)$$

13) $\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$

$$\begin{aligned} \cos(\alpha - \beta) &= \cos(\alpha + (-\beta)) = \cos \alpha \cos(-\beta) - \sin \alpha \sin(-\beta) \\ &= \cos \alpha \cos \beta + \sin \alpha \sin \beta \end{aligned}$$

14) $\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$